

# CA313 Algorithms and Complexity

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	<b>First 6 Weeks</b>	<b>Last 6 Weeks</b>
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## Course webpage:

<http://www.computing.dcu.ie/~away/CA313>

**Recommended Texts:** *"Elements of the Theory of Computation"*, H.R. Lewis & C.H. Papadimitriou, Prentice Hall, 1998 (2nd edition), [511.3/LEW]  
*"Introduction to the Theory of Complexity"*, D.P. Bovet & P. Crescenzi, Prentice Hall, 1994 [511.3/BOV]  
*"The Theory of Computation"*, B.M. Moret, Addison-Wesley, 1998, [511.3/MOR]  
*"Models of Computation"*, J.E. Savage, Addison-Wesley, 1998, [004/SAV]  
*"The New Turing Omnibus"*, A.K. Dewdney, Freeman & Co., 1989, [004/DEW]

# Schedule

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## Lectures

Day	Time	Location
Mon	14:00	QG22
Tues	13:00	QG22

## Assessment

Component	Weight
In-Class Tests	20%
End-of-year exam	80%

The in-class tests will take no more than 45 mins and will be regularly scheduled throughout the semester.

The exam in January will consist of 3 questions (probably out of a choice of 4 or 5).

# What is this Course about?

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“Computer Science is no more about computers than astronomy is about telescopes.” - Edsger W. Dijkstra

- Building on CA215 Languages and Computability, in this course we will develop a framework to classify a program as tractable or intractable.
- A tractable problem has a ‘*fast*’ algorithm that solves **all** instances of the problem.
- An intractable problem can only be solved in the worst case by *brute force* search.

# Polynomial vs. Exponential

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Assume we have a (slow!) computer that carries out 1MIPS. What are the running times (in seconds, unless otherwise stated) for (hypothetical) algorithms of different size inputs  $n$ ?

	10	20	30	40	50	60
$n$	.00001	.00002	.00003	.00004	.00005	.00006
$n^2$	.0001	.0004	.0009	.0016	.0025	.0036
$n^3$	.001	.008	.027	.064	.0125	.0216
$2^n$	.001	1.0	17.9 mins	12.7 days	35.7 years	366 centuries
$3^n$	.059	58 mins	6.5 years	3855 centuries	$2 \times 10^8$ centuries	$1.3 \times 10^{13}$ centuries

Note that the age of the Universe is estimated as  $14 \times 10^9$  years ...

## Course Outline

1. Basic Introduction
  - Mathematical Prerequisites
  - Chomsky Hierarchy
  - Turing Machines
2. Complexity Measures
  - the Class P
  - the Class NP